# RHIC polarization for Runs 9-15

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# 1 Introduction

This note describes the RHIC polarization measurements for use by the collider experiments for the Run9<sup>1</sup> and later polarized proton running periods. The measurement procedure is outlined [1] and the resulting polarization parameters are defined. The systematic uncertainties for each step of the procedure are discussed and estimated; when possible the uncertainties are evaluated using the present data. Finally the use of the provided results to determine mean polarization and uncertainty for a data set is described. The results used for this are compiled on the web pages linked at https://wiki.bnl.gov/rhicspin/Results; there, for each year the results are at the link 'Fill by fill results'.

This is an extension of an earlier note for Runs 9-12 [2], with additional clarifications and the new Run 13 and 15 results. A full list of the data sets presented here is in Table 1.

RHIC Run	$E_p \text{ (GeV)}$	species
9	100	pp
11	250	pp
12	100	pp
12	255	pp
13	255	pp
15	100	pp
15	104	pAu
15	104	pAl

Table 1: Data sets covered in this note.

<sup>&</sup>lt;sup>1</sup>Earlier polarization values for Run9 100 GeV are consistent with the present analysis. The Run9 250 GeV polarization values were not reevaluated, because severe rate effects rendered the data unsuitable for analysis in the present framework.

# 2 Measurement procedure

# 2.1 Proton carbon polarimeters

The proton carbon (pC) polarimeters provide the basis of the polarization measurements. They supply the following information:

- The intensity averaged polarization of the beam,  $P = \int d^2x P(\vec{x})I(\vec{x})/\int d^2x I(\vec{x})$ , where  $\vec{x} = (x, y)$  are the transverse beam coordinates, and  $P(\vec{x})$  and  $I(\vec{x})$  are the transverse polarization and intensity distributions, respectively.
- The transverse polarization profile parameter  $R = \sigma_I^2/\sigma_P^2$ , the square of the ratio of the widths of the beam intensity and polarization distributions; the two pC polarimeters in each RHIC ring allow separate measurements of R in the horizontal and vertical directions;
- With two or more measurements per RHIC fill the pC polarimeters measure the time dependence of P and R throughout fills, necessary for physics data collected during portions of fills;
- The two pC polarimeters in each RHIC ring allow cross checks with two independent measurements of the same beam.

The polarization is obtained from the measured asymmetry  $\epsilon$  via the relation  $P = \epsilon/A_N$ . The analyzing power  $A_N$  is determined separately for each pC polarimeter by normalizing to the hydrogen jet (H-jet) polarimeter absolute polarization values. Uncertainties from the H-jet thus contribute to a scale uncertainty on the pC measurements through the uncertainty in determining  $A_N$ .

The polarizations for single- and double-spin asymmetry (SSA and DSA) measurements with colliding beams are determined from the transverse averaged polarization P and profile parameter R. The corrections from P to  $P_{SSA}, P_{DSA}$  are scale factors which are algebraic functions of R [3]. For equal horizontal and vertical profiles R, to lowest order in R:

$$P_{SSA} \approx (1 + \frac{1}{2}R)P; \tag{1}$$

If both beams B and Y have equal profiles R, to lowest order in R:

$$P_{DSA}^2 \approx (1+R)P_B P_Y \approx P_{SSA,B} \cdot P_{SSA,Y} \,. \tag{2}$$

The pC measurements for a fill are a set of polarization and profile values  $P_i$  and  $R_i$ , their statistical uncertainties, and times in the fill  $t_i$ . They are fit to the forms:

$$P(t) = P_0 - P' \cdot t, \tag{3}$$

$$R(r) = R_0 + R' \cdot t. \tag{4}$$

 $P_0$ ,  $R_0$  are the polarization and profile at t=0, usually taken as the start of a physics fill; P' is the absolute rate of polarization loss and R' is the rate of profile growth. These fits are performed for each pC polarimeter in use; when both polarimeters in a ring are used, their fit parameters and uncertainties are combined in a weighted average to produce a linear parameterization for each beam. For the many short fills, due e.g. to beam loss, with only one pC measurement, the average values of P' and R' over the whole running period are used.

The parameters  $\{P_0, P', R_0, R'\}$  are then used to determine a parameterization of the colliding beam polarizations linear in t; e.g. for SSA:

$$P_{SSA}(t) = P_{0,SSA} - P'_{SSA} \cdot t. \tag{5}$$

Here  $P_{0,SSA}$  and  $P'_{SSA}$  have analogous meanings to the parameters in Eq. (3); their statistical uncertainties are determined by the statistical uncertainties on  $\{P_0, P', R_0, R'\}$ . The DSA polarization is the product of these  $P_{SSA}$  parameterizations for the two beams as indicated in Eq. (2).

# 2.2 H-jet polarimeter

A polarized atomic hydrogen jet is used to measure the absolute polarization of the beam. In terms of measured asymmetries  $\epsilon$  with respect to the jet and the beam spin states, the transverse averaged polarization of the beam is determined:

$$P_{\text{beam}} = -\frac{\epsilon_{\text{beam}}}{\epsilon_{\text{iet}}} P_{\text{jet}}.$$
 (6)

The polarization of the hydrogen jet  $P_{\text{jet}}$  is measured with a Breit-Rabi polarimeter. It is largely constant, and a mean value is used for each running period.

The H-jet polarimeter measures the beam intensity weighted average of  $P_{\text{beam}}$  over a fill:

$$P_{\mathrm{H-jet}} \equiv \overline{P_{\mathrm{beam}}} = \frac{\int dt I(t) P(t)}{\int dt I(t)},$$
 (7)

where  $P_{\mathrm{H-jet}}$  is the result from the H-jet for each beam in each fill.

# 2.3 pC/H-jet normalization

To compare directly with the jet measurement, the beam intensity weighted average polarization from the pC is computed for each fill in terms of the parameterization in Eq. (3):

$$\overline{P_{\text{pC}}} = \left(1 - \left(\frac{P'}{P_0}\right) \cdot \frac{\int dt \, tI(t)}{\int dt \, I(t)}\right) P_0. \tag{8}$$

Note that the ratio  $P'/P_0$  is independent of the pC polarization scale. The RHIC archive values of beam intensities are used to numerically evaluate the terms involving I(t).

Over a set of fills (typically an entire running period) the relative pC/H-jet normalization is determined from a statistically weighted mean of the ratio:

$$s = \left\langle \frac{\overline{P_{\text{pC}}}}{P_{\text{H-jet}}} \right\rangle_{\text{fills}}.$$
 (9)

The scale factor is then applied to all pC polarization values to adjust them to the scale set by the H-jet.

A separate normalization was determined for each pC polarimeter for each running period, using all fills with both pC and H-jet measurements. For the Blue downstream pC polarimeter in Run11, a set of fills when a thick carbon target was used showed a significant deviation in scale; a separate normalization was determined for these data.

## 2.4 Special treatment Run13

## 2.4.1 Spin tilt correction

It is important to note the measurement capabilities of the pC and H-jet polarimeters:

- The pC polarimeters have six detectors arranged azimuthally around the proton beam. This allows a measurement of the spin vector in the plane transverse to the beam; thus, the polarization may be expressed as a magnitude P and tilt angle at the pC polarimeters  $\phi_{pC}$ , where  $\phi_{pC} = 0$  for a vertical spin vector.
- The H-jet has only two detector stations in the horizontal plane of the beam. Thus, asymmetries between these two detector stations measure only the vertical component of the spin vector at the H-jet,  $P\cos\phi_{\rm H-jet}$ .

The normalization procedure followed in previous analyses [2] assumed  $\phi_{H-jet} = 0$ .

Careful analysis of the Run13 255 GeV polarization measurements showed that there were nonzero tilt angles in both beams, with  $\phi_{\rm pC}=16^{\circ}$  for the Blue beam and  $\phi_{\rm pC}=9^{\circ}$  for the Yellow beam [4]. Also, spin tracking analysis shows that the spin vector tilt does not change significantly in the 71 m between the pC and H-jet polarimeters [5], *i.e.*  $\phi_{\rm H-jet}=\phi_{\rm pC}$ . Thus, the H-jet measurements under-measured the Blue beam polarization magnitude by  $\approx 4\%$  and the Yellow beam by  $\approx 1\%$ . The normalization procedure for the Run13 255 GeV data was corrected for this effect<sup>2</sup>.

#### **2.4.2** $P_0$ from H-jet

In Run13 the pC polarimeters experienced a high loss of carbon ribbon targets, requiring two replacements of the target sets during the run. This resulted in a few periods when

<sup>&</sup>lt;sup>2</sup>Subsequent analysis of the older data sets showed that the Run12 255 GeV period had similar spin tilts in both beams; the tabulated polarization results for this period have not been corrected for this effect. The other periods studied did not have significant spin tilts.

there were no viable targets and thus no pC measurements for one of the beams. Many fills in these periods were long enough to provide a statistically significant H-jet measurement. As described in section 2.2, the H-jet measures the beam intensity averaged polarization throughout a fill:

$$P_{\mathrm{H-jet}} = \frac{\int dt I(t) P(t)}{\int dt I(t)} = P_0 + P' \cdot \frac{\int dt \, t I(t)}{\int dt I(t)}, \tag{10}$$

where I(t) is the beam intensity throughout a fill. This allows a determination of the initial polarization for experiments, using run average values for unmeasured parameters:

$$P_{0,SSA} = \left(P_{\text{H-jet}} - \overline{P'} \cdot \frac{\int dt \, tI(t)}{\int dt I(t)}\right) \cdot \left(1 + \frac{1}{2}\overline{R_0}\right). \tag{11}$$

Here  $\overline{P'}$  is the Run13 average of polarization decay, and  $\overline{R_0}$  the Run13 average of initial profile parameter. RHIC archive values of beam intensities are used to numerically evaluate the term involving I(t). The values of  $P_{0,SSA}$  so determined are included in the tabulated results, highlighted in red.

# 3 Uncertainties

## 3.1 H-jet scale and background

The scale of the H-jet polarization is provided by the Breit-Rabi polarimeter measurement of the jet polarization. It may be affected by contamination of the jet with molecular hydrogen H<sub>2</sub>. This was measured in a test bench configuration to be approximately 2%, and the Breit-Rabi measurement is corrected for this. Since this measurement was performed only once several years ago, and never *in situ*, the uncertainty on polarization scale from this effect is conservatively taken to be 3%.

Equation (6) depends on the asymmetries having the same analyzing power with respect to beam and jet polarizations. If backgrounds contribute differently to the beam and jet asymmetries the relation may be invalid. Analysis of the H-jet signal and background regions indicates that possible backgrounds contribute less than 1% to beam or jet asymmetries, providing an upper limit to the violation of Eq. (6). For Run15 the backgrounds were explicitly subtracted leaving negligible uncertainties.

# 3.2 pC scale

The pC/H-jet ratios  $\overline{P^{pC}}/\overline{P^{jet}}$  [6] averaged in Eq. (9) are proportional to the pC analyzing power  $A_N$ . This should be constant within uncertainties. If fit to a constant using only statistical uncertainties, a value of  $\chi^2/NDOF > 1$  indicates fill-to-fill systematic uncertainties on the ratios; these effects may be due to instabilities in either the pC or H-jet or both. The size of this effect may be estimated by including a constant systematic for each

fill in the  $\chi^2$  calculation and requiring  $\chi^2/NDOF=1$ . The values so obtained are listed in Table 2. Many of them are zero, indicating the systematic uncertainty is negligible in comparison to the statistical uncertainties with typical values of  $\approx 9\%$ . Asterisks in table entries indicate when there were known instabilities in a polarimeter; these account for many of the nonzero values.

$\sigma(P)/P$ (%)	B up	B dn	Y up	Y dn
Run9-100	0.	0.	0.	0.
Run11-250	2.6	2.5*	0.	0.*
Run12-100	0.	0. *	6.4*	0.*
Run12-255	0.	3.3*	5.6*	3.3*
Run13-255	0.	0.	0.	6.6
Run15-100 pp	0.	0.	0.6	4.3
Run15-104 pAu	5.	0.	-	-
Run15-104 pAl	0.	0.	-	-

Table 2: Relative fill-to-fill systematic uncertainties on the pC/H-jet ratio. Asterisks indicate there were known instabilities in a pC polarimeter.

After including possible systematic uncertainties, the mean in Eq. (9) is re-evaluated, with a possibly increased uncertainty. The overall relative uncertainties on this mean are listed for the individual polarimeters in the left columns of Table 3. For most fills the polarization of one beam is the average of the up- and downstream polarimeters; the relative uncertainty on  $A_N$  for this average is listed in the rightmost two columns of Table 3. These are also the overall relative uncertainties on  $A_N$ , and contribute a scale uncertainty to the pC measurements. They incorporate the statistical uncertainties of the H-jet and pC from an entire running period, and all fill-to-fill systematic uncertainties from both.

$\sigma(A_N)/A_N$ (%)	B up	B dn	Y up	Y dn	Blu	Yel
Run9-100	1.6	1.1	1.2	1.1	1.0	0.8
Run11-250	1.4	1.8	1.3	1.7	1.1	1.1
Run12-100	1.3	2.0	2.0	1.5	1.2	1.3
Run12-255	1.3	2.2	2.0	1.6	1.3	1.3
Run13-255	1.0	0.9	1.0	1.1	0.7	0.8
Run15-100 pp	0.6	0.6	0.6	0.8	0.4	0.5
Run15-104 pAu	1.2	0.9	-	-	0.7	-
Run15-104 pAl	1.7	1.6	-	-	1.1	-

Table 3: Overall relative uncertainties (stat.  $\oplus$  syst.) on the pC analyzing power  $A_N$ .

## 3.3 pC fill-to-fill scale systematics

The pC analyzing power  $A_N$  has a steep dependence on the energy of the scattered carbon nuclei; the measurement is thus sensitive to the energy scale of the measured nuclei. Leading sources of systematic shifts in this energy scale include the dead layer of the Si detectors, and varying energy loss of nuclei in the carbon target en route to the detectors.

For most fills each RHIC beam has (intensity averaged) polarization measurements from both the up- and down-stream pC polarimeters. Measuring the same beam, they should yield the same polarization, within uncertainties [7]. Possible fill-to-fill systematic uncertainties may be estimated by requiring the ratio to be consistent with unity, adjusting  $\chi^2/NDOF = 1$  as described in Section 3.2. The contribution of these uncertainties to the polarization scale are listed in Table 4. They are small or negligible compared to the statistical uncertainties on the ratios from each fill with typical values of 10%. Note also that these uncertainties are already incorporated in the uncertainties on  $A_N$  in Table 3 through the pC/H-jet ratio used to determine  $A_N$ .

$\sigma(P)/P$ (%)	Blu	Yel
Run9-100	0.	1.0
Run11-250	3.2	0.9
Run12-100	0.	2.8
Run12-255	0.	3.1

$\sigma(P)/P$ (%)	Blu	Yel
Run13-255	2.8	1.4
Run15-100 pp	0.	0.
Run15-104 pAu	1.3	-
Run15-104 pAl	0.	-

Table 4: Relative fill-to-fill systematic uncertainties on the pC polarization as estimated from the upstream/downstream ratio.

#### 3.4 Profile correction procedure systematics

The profile parameter R is determined from a fit of the polarization versus intensity (rate) distribution:  $P(I) = P_{max} \cdot (I/I_{max})^R$  [8]. The fit parameters  $P_{max}$  and R determine  $P_{avg}$ , the average polarization across the beam:  $P_{avg} = P_{max}/\sqrt{1+R}$ . This may be compared to the directly measured average from a sweep measurement P; differences are due to systematic effects of the profile correction procedure. This is used to estimate the uncertainty of the correction for colliding beams. Based on this study the fill-to-fill relative uncertainty on the profile correction is 2.2%.

# 4 Use of results

## 4.1 Tabulated parameters

The results of the polarization measurements are compiled on web pages [9]. Polarization values and statistical uncertainties for SSA with each beam are listed. For each the initial value and slope of the parameterization  $P(t) = P_0 - P' \cdot t$  are provided<sup>3</sup>; a Unix time stamp value for t = 0 in this parameterization is also included. When there was only one polarization measurement in a fill, the mean values of P' and R' for that ring and running period are used. A beam current weighted mean polarization is also listed:  $P_{\text{Avrg}} = \int dt I(t)P(t)/\int dt I(t)$ .

# 4.2 Mean polarization

For each fill i in a data set a time dependent luminosity  $L_i(t)$  is required; it should include effects such as deadtimes, varying trigger prescales etc. The appropriate  $P_i(t)$  from the web page is also needed. When available the initial and slope values should be used:  $P_i(t) = P_{0,i} - P'_i \cdot t$ . Fills with only a mean polarization were typically short and may be approximated as a constant:  $P_i(t) = P_{\text{Avrg},i}$ . It is convenient to define the mean luminosity weighted polarization for fill i:

$$\mathcal{P}_i = \frac{1}{\mathcal{L}_i} \int dt L_i(t) P_i(t) = P_{0,i} - \frac{\int dt \, t L_i(t)}{\mathcal{L}_i} P_i', \tag{12}$$

where  $\mathcal{L}_i = \int dt L_i(t)$  is the total luminosity for fill *i*. Then the polarization for the data set is determined from the luminosity weighted average over fills *i*:

$$P_{set} = \frac{\sum_{i} \mathcal{L}_{i} \cdot \mathcal{P}_{i}}{\sum_{i} \mathcal{L}_{i}}.$$
 (13)

#### 4.3 Polarization uncertainty

There are several contributions to the overall uncertainty on P. Each component may vary according to ring and running period. It is convenient to separate them into an overall scale uncertainty for a given running period, and a fill-to-fill uncertainty for subsets of a running period.

#### 4.3.1 Overall scale uncertainty

The contributions to the overall scale uncertainty are:

<sup>&</sup>lt;sup>3</sup>The slope values listed in the tables ('Slope' or 'dP/dT' ) are opposite in sign from P' in this note.

- H-jet scale: For SSA measurements the relative uncertainty on scale from the Breit-Rabi jet measurement is  $\sigma(\text{H-jet scale})/P = 3\%$ . For DSA, the scale is fully correlated between the two beams and  $\sigma(\text{H-jet scale})/P = 6\%$ .
- H-jet background: The upper limit on background contribution to asymmetries is taken as the uncertainty on the H-jet polarization; for SSA,  $\sigma(\text{H-jet bkg})/P = 1\%$ . For DSA the effect is fully correlated and  $\sigma(\text{H-jet bkg})/P = 2\%$ . For Run15 the backgrounds were explicitly subtracted leaving negligible uncertainties.
- pC scale: The appropriate value for  $\sigma(pC \text{ scale})/P$  for each beam is listed in the rightmost two columns of Table 3. For DSA the uncertainties for the two beams are uncorrelated and are added in quadrature,  $\sigma(pC \text{ scale})/P = \sigma(Blu-pC \text{ scale})/P \oplus \sigma(Yel-pC \text{ scale})/P$ .

The contributions are added in quadrature, giving the relative scale uncertainties for each running period listed in Table 5.

$\sigma(\text{scale})/P$ (%)	SSA-Blu	SSA-Yel	DSA
Run9-100	3.3	3.3	6.5
Run11-250	3.3	3.3	6.5
Run12-100	3.4	3.4	6.6
Run12-255	3.4	3.4	6.6
Run13-255	3.2	3.3	6.4
Run15-100 pp	3.0	3.0	6.0
Run15-104 pAu	3.1	-	-
Run15-104 pAl	3.2	-	-

Table 5: Overall scale relative uncertainties on polarization.

## 4.3.2 Fill-to-fill uncertainty

The contributions to the fill-to-fill uncertainty are:

• Fill-to-fill scale systematics: Equations (12,13) may be used to determine the fill-to-fill uncertainty on P through usual propagation of errors, taking the statistical uncertainties on  $P_{0,i}, P'_i$  or  $P_{\text{Avrg},i}$  from the web page. The systematic uncertainties from Table 4 should be added to the statistical uncertainties in quadrature, adding the Blu and Yel values in quadrature for DSA. For example,

$$\sigma(\mathcal{P}_i) = \sigma(P_{0,i}) \oplus \frac{\int dt \, t L_i(t)}{\mathcal{L}_i} \cdot \sigma(P_i') \oplus \mathcal{P}_i \cdot (\sigma(P)/P)_{\text{Table 4}}$$
(14)

and

$$\sigma(P_{set}) = \frac{\bigoplus_{i} \mathcal{L}_{i} \cdot \sigma(\mathcal{P}_{i})}{\sum_{i} \mathcal{L}_{i}}.$$
(15)

However, this leads to double counting of uncertainties, since they already contribute to  $\sigma(\text{scale})$  through the uncertainties on  $A_N$  in Table 3. (Recall that the uncertainties on  $A_N$  incorporate all statistitical and systematic uncertainties from both the H-jet and pC for an entire running period, as described in Section 3.2.) The  $A_N$  were evaluated using nearly entire run periods, so the overcounting is significant when the data set used for a measurement is an appreciable fraction of the run period. An approximate correction for the overcounting should be applied; since the errors are fill-to-fill the correction depends on the numbers of fills used. Suppose that N fills in the entire run period were used to determine  $A_N$ ,  $M \leq N$  fills are in the data set for the measurement, and let  $\sigma(15)$  be the uncertainty determined from Eq. (15). Then the corrected uncertainty is  $\sigma(\text{fill-to-fill scale}) = \sqrt{1 - \frac{M}{N}} \sigma(15)$ . The values of N for each running period are listed in Table 6. In each period there were several fills not used for the determination of  $A_N$ , ususally because the fills were short and the statistics were too limited for an H-jet measurement. Thus it is possible that M > N; in these cases it is reasonable to take  $\sigma(\text{fill-to-fill scale}) = 0$ .

N  (# fills)	Blu	Yel
Run9-100	117	116
Run11-250	65	65
Run12-100	56	55
Run12-255	49	49

N  (# fills)	Blu	Yel
Run13-255	138	139
Run15-100 pp	142	142
Run15-104 pAu	80	-
Run15-104 pAl	30	-

Table 6: Number of fill used to determine  $A_N$ .

• Profile correction: The relative uncertainty of the profiles correction for one beam in one fill is 2.2%. For a set of M fills it contributes a relative uncertainty on the polarization for an SSA measurement of  $\sigma(\text{profile})/P = 2.2\%/\sqrt{M}$ , and for a DSA measurement  $\sigma(\text{profile})/P = 3.1\%/\sqrt{M}$ .

For data sets consisting of a large fraction of a running period the fill-to-fill systematic uncertainties are negligible.

#### 4.3.3 Total uncertainty

These components of the uncertainty are then added in quadrature to give the overall uncertainty on  $P_{set}$ . Explicitly, in terms of  $\sigma(\text{scale})/P$  from Section 4.3.1, and  $\sigma(\text{fill-to-fill scale})$ 

and  $\sigma(\text{profile})/P$  from Section 4.3.2, the total uncertainty on the mean polarization for a data set is

$$\sigma(P_{set}) = P_{set} \cdot \frac{\sigma(\text{scale})}{P} \oplus \sigma(\text{fill-to-fill scale}) \oplus P_{set} \cdot \frac{\sigma(\text{profile})}{P} . \tag{16}$$

For data sets consisting of a large fraction of a running period the fill-to-fill systematic uncertainties are negligible and  $\sigma(P_{set})/P_{set} = \sigma(\text{scale})/P$  from Table 5.

## 4.3.4 Scale uncertainty of different running periods

The polarization scale uncertainty is dominated by the 3% uncertainty on  $H_2$  contamination of the polarized atomic hydrogen jet, discussed in Section 3.1. Within a given running period, the pC configuration was fixed, and the pC/H-jet normalization is sensitive to fluctuations in the  $H_2$  contamination. As summarized in Section 3.2 and Table 2, systematic fill-to-fill variations of the ratio were usually negligible or less than 3%; when they were larger than 3%, the fluctuations may be attributed to known instabilities of the pC polarimeter. Thus, within a running period the fluctuations in  $H_2$  contamination were within the 3% uncertainty.

In different running periods, the pC configuration was altered, and the pC/H-jet ratios are not directly comparable. Also, there were no direct measurements of the jet  $\rm H_2$  contamination in different running periods; the 3% uncertainty was assigned to span likely variations of the contamination between different periods. Given the lack of information, it is prudent to choose a maximally conservative estimate of the scale uncertainty when combining data from different running periods. This depends on whether identical or different measurements are being combined. Consider the example of a process measured in different kinematic regions A and B. Then:

- If region A was measured in both Run11-250 and Run12-255, select the larger of the uncertainties from Table 5, 3.4% in this case.
- If region A was measured in Run11-250, and region B in Run12-255, assign the relevant uncertainties from Table 5 to each, in this case 3.3% for A and 3.4% for B.

## References

- [1] Much more information on the polarimetry system is available on the polarimetry wiki and links therein: https://wiki.bnl.gov/rhicspin/Polarimetry. The tabulated polarization results are compiled on the web pages linked at https://wiki.bnl.gov/rhicspin/Results; there, for each year the results are at the link 'Fill by fill results'.
- [2] http://public.bnl.gov/docs/cad/Documents/RHIC polarization for Runs 9-12.pdf.

- [3] W. Fischer and A. Bazilevsky, Phys. Rev. ST Accel. Beams 15, 041001 (2012).
- [4] http://www.cadops.bnl.gov/AP/spinmeeting.htm, see Feb. 25, 2015 meeting minutes and presentation 'Tilt Spin?'.
- [5] Ibid., see Feb. 25, 2015 meeting minutes and presentation 'Is It Possible?'.

or 'Y1D'.

- [6] An example of the H-jet/pC ratios for the Blu upstream polarimeter in Run12 255 GeV running is at:

  http://www.phy.bnl.gov/cnipol/runs/run12\_e255/images//runs/B1U/c\_hNormJCVsFill\_B1U\_255.png .

  Other running periods are available by replacing 'Run12' with 'Run11' or 'Run09', and '255' with '100' or '250'; other polarimeters by replacing 'B1U' with 'B2D, 'Y2U'
- [7] An example of the upstream/downstream ratios for the Blu pC polarimeters in Run12 255 GeV running is at:

  http://www.phy.bnl.gov/cnipol/runs/run12\_e255/images//runs/BLU/c\_hPolarRatioSystVsFill\_BLU\_255.png .

  Other running periods are available by replacing 'Run12' with 'Run11' or 'Run09', and '255' with '100' or '250'; other polarimeters by replacing 'BLU' with 'YEL'.
- [8] An example of a distribution of polarization vs. intensity and fit from one pC measurement is at:

  http://www.phy.bnl.gov/cnipol/runs/16720.005/images//profile/c\_hPolarVsIntensProfile.png.
- [9] The results are available at https://wiki.bnl.gov/rhicspin/Results; there, for each year click on 'Fill by fill results'.